

1. Data Representation

13.1 User-defined Data Types

Purpose of user defined data types

- To create a new data type
- To allow construction of data types not available in a programming language (extends flexibility of a programming language)
- Constructed by the programmer

Composite

- Collection of data that consists of multiple elements of different (or the same) data types which are grouped under a single identifier
- Can be user-defined or primitive
- Contain more than one data type in their definition
- Includes a record, set and class/object

Record

- Uses other data types in its definition to form a single new one
- Data types referenced can be primitive or user-defined
- Includes related items and a fixed number of items

TYPE *record_name*

 DECLARE *field_name1* : DATA TYPE

 DECLARE *field_name2* : DATA TYPE

 DECLARE *field_name3* : DATA TYPE

ENDTYPE

Set

- Includes a list of unordered elements
- Theory operations (such as intersection or union) can be applied to its elements
- Includes the data type it stores as part of its definition
- All elements are of the same data type

TYPE <*identifier*> = SET OF DATA TYPE

DEFINE <*set_name*> = (*value1, value2, value3, ...*) : <*identifier*>

Non-Composite

- Can be defined without referencing another data type
- Can be a primitive type available in a programming language or a user-defined type
- Contains only one data type in their definition
- Includes a pointer and any primitive/enumerated data type
 - Enumerated Data Type – has an ordered list of all possible values
 - Pointer Data Type – used to reference a memory location, stores addresses/memory locations and indicates the type of data stored there

(Pseudocode for Non-Composite Data Types)

- Enumerated

TYPE <identifier> = (value1, value2, value3, ...)

TYPE Season = (Spring, Summer, Autumn, Winter)

- Pointer

TYPE <identifier> = ^DATA TYPE

TYPE IntPtr = ^INTEGER

13.2 File Organisation and Access

File Organisation Methods

Serial Files

- Records are stored one after the other in chronological order
- New records are appended to the end of the file
- When searching – every record needs to be checked until the record is found or all have been checked
- Examples include...
 - Creating unsorted/temporary transaction files
 - Creating data logging files

Sequential Files

- Files are stored and addressed one after the other
- A new version of the file has to be created to update it
- Files are stored with ordered records – records are stored in order of the key field
- New records are inserted in the correct position
- When searching – the key field is compared and every record is checked until it is found, or the key field of a current record is greater than the one being searched for

Random Files

- Records are stored in no particular order within the file (there is no sequencing)
- There is a relationship between the record key and its location within the file – the location of the record is found using a hashing algorithm
- Updates to the file can be carried out directly

File Access Methods

Sequential Access Process (For Sequential and Serial Files)

- Records are checked linearly until the desired record is found/end of file is reached
- Starts searching for records one after the other from the physical start of the file until the record is found or the end of the file is reached
- Most suitable when data is stored in a certain order based on a field – e.g. bank stored data records in ascending order of account number

Direct (For Sequential and Random Files)

- Most suitable when a record is referenced by a unique address
- Allows a record to be found in a file without other records being read – records are found by using the key field of the target record (the record's location is found using a hashing algorithm)
- Sequential Files
 - an index of all key fields is kept – the index is searched for the address of the file location where the target record is stored
- Random Files
 - a hashing algorithm is used on the key field of the record to calculate address of the memory location where the target record is expected to be stored
 - Linear probing or Search overflow can be used to find a record if it is not at the expected location

Hashing algorithm

- Used in direct access methods on random and sequential files
- Is a mathematical formula - performs a calculation on the key field of a record
- Result of calculation gives the address of the memory location where the record is located/should be stored

Hash Value Duplicates (a calculated hash value is a duplicate of another value for a different record key)

Collisions

- occurs when two values/data items in the key field for two records result in the same hash value (when passed through a hashing algorithm)
- Means the storage location identified by the algorithm may already be in use by another record – two records cannot occupy the same address

Process of Collision Resolution

- When storing a record
 - Linear progression - record is stored in next free memory space after the one identified by the hashing algorithm
 - Record is stored in the next free memory space in the overflow area
- When finding a record

→ search the overflow area linearly until the matching record key is found (if not found, record is not in file)

13.3 Floating-point Numbers, Representation and Manipulation

Changing the bit allocation

- When the number of bits in the mantissa is raised, the precision/accuracy of the represented number increases – when the bit number is lowered, the accuracy is reduced
- When the number of bits in the exponent is raised, the range of possible numbers can be represented is increased – when the bit number is lowered, the range decreases

Why binary numbers are stored in normalised form

- To store a maximum range of numbers in a minimum number of bytes/bits
- Normalisation minimises the number of leading 0/1s represented (Numbers whose mantissa begins with 10 or 01 are normalised)
- Maximises the number of significant bits – increases precision/accuracy when storing very small/large numbers
- Avoids the possibility of many numbers having multiple representation

Storing floating point numbers

- Large numbers require a greater number of bits for the mantissa

Overflow

- Occurs following an arithmetic/logical operation – result is too large to be precisely represented in the available system
- Numbers cannot be stored accurately in certain computer systems if they require more bits than is available

Underflow

- Occurs following an arithmetic/logical operation – the result is too small to be precisely represented in the available system (number does not have enough bits to be represented)

**always refer to the loss in precision and state the number/digits would be truncated*

Why A Binary Number Is Sometimes An Approximation

- Real (decimal) numbers can have a fractional part
- Binary numbers have limited fractional representation (limited to powers of 2)

- Fixed length of storage means you can't store very large/small numbers – it's not possible to store all fractions with the level of precision that is provided

Converting between denary and floating-point binary

$M \times 2^E$ where M is the mantissa and E is the exponent

Both are always in two's complement (There is a binary point following the -1 in the mantissa)

Mantissa Representation:

-1	1/2	1/4	1/8	1/16	1/32	1/64	1/128

Exponent Representation:

-128	64	32	16	8	4	2	1

- Floating-point binary → Denary
 1. Convert the number in the exponent to denary
 2. Shift the mantissa binary point to the right by the number held in the exponent
 3. Convert to binary, where numbers after the point are $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$ and so on...

E.g. 01011010 x 00000100

→ 00000100 = 4

→ 0.1011010 - point shifts 4 places right

→ 01011.010 = 1 + 2 + 8 + $\frac{1}{4}$ = 11.25

- Denary → Floating-point binary

1. Convert the number into binary, separating fractions using a binary point
2. Move the binary point left until only one digit comes before it, counting the amount of places the point moves up (gives you the exponent)

Eg. 4.75

→ $4.5 = 4 + \frac{1}{2} + \frac{1}{4} = 0100.11$

→ $0100.11 \rightarrow 0.10011$ - point is shifted 3 places left, hence the exponent is 3

→ $3 = 0011$, so the final number is 010011×0011